

1. EXERCISE SET 3.1

†2b: Yes:  $6r + 4s^2 + 3 = 2(3r + 2s^2 + 1) + 1$ , where  $3r + 2s^2 + 1$  is an integer (since  $r$  and  $s$  are integers). Therefore, it is odd, by definition.

4: Yes: for  $a = b = 0$ , we have  $\sqrt{0+0} = 0 = \sqrt{0} + \sqrt{0}$ .

†9: The values of  $n^2 - n + 11$  for  $1 \leq n \leq 10$  are (in order): 11, 13, 17, 23, 31, 41, 53, 67, 83, 101, which are all prime numbers.  $\square$

†12: Let  $m$  and  $n$  be two odd numbers. By definition,  $m = 2k + 1$  and  $n = 2l + 1$ , for some integers  $k$  and  $l$ . Adding the two equations yields:  $m + n = 2k + 1 + 2l + 1 = 2(k + l + 1)$ , which is even, by definition.  $\square$

†16: For instance, take  $a = -5$ ,  $b = 2$ . Then  $a < b$ , but  $a^2 = 25 \not< 4 = b^2$ .

35: For instance, take  $n = 11$ . Then  $n^2 - n + 11 = 11^2$ , which is not prime.

2. EXERCISE SET 3.2

†2:  $39602/10000 = 19801/5000$

†15: Let  $m = \frac{a}{b}$  and  $n = \frac{c}{d}$  be any two rational numbers. The difference is

$$m - n = \frac{a}{b} - \frac{c}{d} = \frac{ad}{bd} - \frac{bc}{bd} = \frac{ad - bc}{bd},$$

which is a rational number.  $\square$