

The value of a computer, or an automobile, or a machine *depreciates* (decreases) over time. **Linear depreciation** means that the value of the item at time  $x$  is given by a linear function  $f(x) = mx + b$ . The slope  $m$  of this line gives the rate of depreciation.

EXAMPLE: According to the *Kelley Blue Book*, a Ford Mustang two-door convertible that is worth \$14,776 today will be worth \$10,600 in two years (if it is in excellent condition with average mileage).

(a) Assuming linear depreciation, find the depreciation function for this car.

Solution: We know the car is worth \$14,776 now ( $x = 0$ ) and will be worth \$10,600 in two years ( $x = 2$ ). So the points  $(0, 14,776)$  and  $(2, 10,600)$  are on the graph of the linear depreciation function and can be used to determine its slope:

$$m = \frac{10,600 - 14,776}{2} = \frac{-4176}{2} = -2088$$

Using the point  $(0, 14,776)$ , we find that the equation of the line is

$$y - 14,776 = -2088(x - 0)$$

$$y - 14,776 = -2088x$$

$$y = -2088x + 14,776.$$

Therefore, the rule of the depreciation function is  $f(x) = -2088x + 14,776$ .

(b) What will the car be worth in 4 years?

Solution: Evaluate  $f$  when  $x = 4$ :

$$f(x) = -2088x + 14,776$$

$$f(4) = -2088(4) + 14,776 = \$6424$$

(c) At what rate is the car depreciating?

Solution: The depreciation rate is given by the slope of  $f(x) = -2088x + 14,776$ , namely, -2088. This negative slope means that the car is decreasing in value an average of \$2088 a year.